End unit effect on the glass transition temperature of low-molecular-weight polymers and copolymers

F. Danusso* and M. Levi

Dipartimento Chimica Industriale & Ingegneria Chimica 'G. Natta', Politecnico di Milano, Piazza Leonardo da Vinci 32, 20133 Milano, Italy

and G. Gianotti and S. Turri

Ausimont SpA, Centro Ricerche Sviluppo (CRS), Bollate, Milano, Italy (Received 5 June 1992; revised 5 January 1993)

Experimental results for five series of linear oligomers of different molecular weights, having a common perfluorinated molecular body and five different pairs of equal foreign end units, generally demonstrate the substantial influence of the chemical nature of the end units on the $T_{\rm g}-x$ relation of polymers and copolymers, with progressive evidence when the molecular weight is lowered. Positive or negative deviations from the body $T_{\rm g}$ asymptotic value are observed with different types of end units. Previous experimental results and theoretical expectations for the $T_{\rm g}$ at low x values are reviewed briefly. As a first approximation, the applicability of the simplest two-parameter $T_{\rm g}-x$ equations to the new results is discussed, as well as the situation when x is translated in terms of end copolymeric composition.

(Keywords: fluorinated polymers; oligomers; glass transition; end groups; copolymers)

INTRODUCTION

The relation between properties and degree of polymerization of low-molecular-weight polymers or copolymers has received considerable attention in the last few years. These compounds have become of interest not only as macromonomers for the synthesis of macromer segmented copolymers, but also directly as chemicals or materials for an increasing variety of applications.

It is common knowledge that when the molecular weight of a polymeric system is lowered, changes in properties are, in general, to be expected as a consequence of the related structural modifications, which can be described in terms of increasing end-group concentration.

In particular, when considering the glass transition temperature $T_{\rm g}$, it is a common view that its value must decrease on decreasing the molecular weight; this is because of the progressive loosening of the cohesive state of the system due to the greater mobility of the end units compared to those of the molecular body (frequently referred to as the 'plasticizing effect' of the end groups).

This view is certainly correct when the end units or groups have chemical similarity to the body units. However, many polymeric or copolymeric systems have end units or groups which are chemically dissimilar to those of the molecular body, either in their intrinsic constitution, or structurally, as a consequence of the method used in their synthesis (polycondensation polymers or copolymers, segmented or graft copolymers,

star polymers, telomers, telechelic oligomers, etc.). Hence, some contribution from this chemical dissimilarity to a complete 'end-group effect' is reasonably to be expected.

The aim of this paper is to review, to demonstrate and to stress the general presence of this type of chemical dissimilarity effect of the end units or groups on the $T_{\rm g}$ (and plausibly on other properties), to determine to what extent it can become a prevailing factor, and yield experimental results which, considering the present state of knowledge, may seem quite unexpected (as it will be illustrated by the brief review that follows).

Alternatively, this contribution to the end effect, specifically due to a difference in the chemical nature of the constituent units, may also be seen as a 'copolymer end effect', which, especially for the lowest molecular weights, tends to become closely related to that typical of triblock copolymeric structures.

T_{g-x} FOR POLYMER AND COPOLYMER SYSTEMS

The $T_{\rm g}-x$ relation of a polymer system, including low-molecular-weight oligomers, is frequently studied by estimating the asymptotic $T_{\rm g}$ value at high molecular weights and taking into consideration the $T_{\rm g}$ deviations from that value at lower molecular weights. Experimental results are sometimes compared with those suggested by theoretical, tractable models, whose development manages to qualitatively or quantitatively account for such deviations.

^{*} To whom correspondence should be addressed

In this brief review, we shall consider, first, systems which are by themselves devoid of an end effect (true homopolymers), namely cyclic polymers; second, systems so far studied disregarding any chemical dissimilarity end effect (linear and star polymers); and finally, systems intentionally studied with chemical dissimilarity end effects (with linear polymeric or copolymeric molecular body), including our new experimental results.

Cyclic polymers

The molecular structure of a cyclic polymer system may be seen, at an infinite molecular weight, as that of a single, infinite linear chain. By decreasing the molecular weight, only minor cohesion energy changes may be forseen, whereas every molecule, being cyclic, intrinsically loses conformational degrees of freedom, increasingly as the length of the cyclic chain diminishes. If the molecular rings happen to be catenated, additional losses of degrees of freedom take place. However, the number of molecules increases in the system, which thus gains degrees of freedom.

For these systems, the first reliable experimental results for the T_g appear to be those of Clarson et al. for cyclic poly(dimethylsiloxane); by decreasing x, moderate positive deviations of $T_{\rm g}$ from the asymptotic value were found, which became noticeable, in a monotonic rise from the asymptote, with x going below about 20.

Positive deviations are also described by Hogen-Esch and Toreki² for cyclic poly(2-vinylpyridine), and again by Clarson et al.3 for cyclic poly(phenylemethylsiloxane).

Theoretical support for these findings is given by Di Marzio and Guttman⁴, based on equilibrium thermodynamics arguments and the evaluation of conformational entropic differences between cyclic (noncatenated) and corresponding linear polymers. Their treatment predicts that, whereas 'linear chains always show a decrease of T_g , as the molecular weight is lowered (see below), cyclic polymers either show a smaller decrease or, more usually, an increase in T_{g} .

Linear polymers

The T_g -x relation of linear polymer systems has been studied by many authors either experimentally or theoretically. The nature of the end units, although not always known precisely, has in general been conceptually considered as not substantially different from that of the body units, except for their inherent greater mobility. For such a model of a polymeric system which may be seen as 'scissor-made' from an infinite chain, on lowering the molecular weight, a kind of 'discohesion' progressively takes place, with a gain of degrees of freedom and a loss of cohesion energy. Hence, a progressive lowering of $T_{\rm g}$ from its asymptotic value is clearly to be expected, with negative T_{g} deviations. This has, as a rule, been confirmed for the systems studied, both by experimental data and theoretical considerations.

The first fully theoretical treatment is that of Gibbs and Di Marzio⁵. By assuming that the glass transition can be dealt with as an equilibrium thermodynamic transition of the Ehrenfest⁶ second-order type, and that the configurational entropy, calculated on a Flory-Huggins lattice model, should be zero along the transition line, an equilibrium value of $T_{\rm g}$ can be predicted (because of relaxation, at about 50 K below the experimental value). From this treatment, a rather complex T_g -x relation could

also be obtained, which proved successful for high to rather low molecular weights with some linear polymer systems 7-11, but unsuccessful with others (see for example ref. 12).

More successful for several systems are simple statements which can be derived as a first approximation from the view of a hole contribution of the chain ends to an 'iso-free-volume state' at T_g , first put forward by Fox and Flory¹³ from experimental data of a polystyrene system, leading to an equation of the type:

$$T_{\rm g} = T_{\rm g}(\infty) - \frac{K}{x} \tag{1}$$

where $T_{\mathbf{g}}(\infty)$ is the $T_{\mathbf{g}}$ asymptotic value at $x \to \infty$, and Kis a positive constant.

Ueberreiter and Kanig¹⁴, with arguments based on their dilatometric results with polystyrene fractions (x from 2 to 928)15 and mixtures of fractions14, found as more adequate, on an essentially empirical ground, an equation of the type:

$$\frac{1}{T_{\rm g}} = \frac{1}{T_{\rm g}(\infty)} + \frac{H}{x} \tag{2}$$

where H is a positive constant. Its validity was reconsidered by Schulz et al. 16 and Fox and Loshaek 17.

Equation (1) is frequently used to represent or discuss experimental data of various systems (see for example refs. 1, 3, 12, 18-21).

Fox and Loshaek¹⁷, further developing volumetric considerations, obtained a more general relation of the

$$T_{\rm g} = T_{\rm g}(\infty) \frac{x - A}{x + B} \tag{3}$$

which can be rewritten in the following two ways:

$$T_{\rm g} = T_{\rm g}(\infty) \left(1 - \frac{A+B}{x+B} \right) = T_{\rm g}(\infty) - T_{\rm g}(\infty) \frac{A+B}{1 + (B/x)} \frac{1}{x}$$
 (4)

$$\frac{1}{T_{\rm g}} = \frac{1}{T_{\rm g}(\infty)} \left(1 + \frac{A+B}{x-A} \right) = \frac{1}{T_{\rm g}(\infty)} + \frac{1}{T_{\rm g}(\infty)} \frac{A+B}{1 - (A/x)} \frac{1}{x}$$
(5)

where A and B are essentially volumetric and dilatometric parameters.

For sufficiently high values of x, equations (4) and (5) reduce to the form of equations (1) and (2) respectively. Considering the possible values of the parameters which express the constants of equations (4) and (5), it may be argued¹⁷ that equation (2) should provide a better approximation than equation (1) for a wider range of x. Rigorously, equations (1) and (2) would be directly derivable from equation (3) if B=0 or A=0 respectively (in the treatment of Fox and Loshaek¹⁷, where A and Bare volumetric parameters, this appears to be physically

Kelley and Bueche²² suggested a simple calculation of the K constant of equation (1) from volumetric quantities and a parametric average hole volume.

Someynsky and Patterson²³, by considering polymers of different x as being in corresponding states at T_g , on the lines of a Prigogine thermodynamic theory of liquids, could obtain directly an equation like equation (2), whose H constant is expressed in terms of molecular flexibility parameters and of a cohesion energy factor accounted

for through the $T_{g}(\infty)$ parametric value (formally, their equation corresponds to equation (3) with A=0, and therefore to equation (2)).

Equation (2) was then systematically interpreted by Kanig²⁴ through a detailed classical thermodynamic treatment of an attractive physical model: the liquid polymer is assumed to be a saturated 'solution' of holes, which becomes oversaturated, because frozen, when, by lowering the temperature, T_g is reached. The corresponding (free) volume is conceived to be due not only to frozen holes, but also to non-freezable thermal vibrations, with a characteristic ratio of the twocomponent free-volume fractions at T_g (about 2:1). This is seen as a universal feature determining T_g , in addition to a factor bound to the energy for creating a hole, which, on the contrary, depends on the nature of the polymer system considered. From generally formulated relations, equation (2) could be interpreted by assuming a similarity in the nature of the end units and the body.

More recently, Lee and Williams²⁵, on the basis of a non-equilibrium thermodynamic theory previously formulated²⁶ and of a generalized definition of thermomechanical transitions, expressed the $T_{\rm g}$ -x relation in the following terms:

$$\ln x = B_0 - \frac{B_1}{T_g}$$
 or $T_g = \frac{B_1}{B_0 - \ln x}$ (6)

where B_0 and B_1 are intrinsically positive constants, the latter being proportional to the activation enthalpy of the transition process. They observed good agreement with the experimental data of Fox and Flory²⁷, Rudin and Burgin²⁸, and Gillham and Boyer^{18,19} for polystyrene, of Beevers and White⁷ for poly(methyl methacrylate), and of Pezzin *et al.*⁹ for poly(vinyl chloride). Marchionni *et al.*²⁹ then found agreement of equation (6) with their experimental results for copolymeric perfluoropolyethers.

However, Di Benedetto³⁰, by assuming that the principle of corresponding states is valid and that a single universal value for the reduced glass transition temperature can be considered, used some additional simplifying assumptions in the calculation of a total lattice energy, and derived an equation of the type:

$$T_{\mathbf{g}} = T_{\mathbf{g}}(\infty) \frac{(a+x)^2}{(b+x)(c+x)} \tag{7}$$

in which a, b and c are constants expressed as ratios between parameters referring to end groups and chain units, respectively bound to interaction energies, segmental mobilities and number of contacts between segments or groups. His treatment explicitly takes into consideration the role of the end groups; however, it could not be checked by adequate experimental data from the point of view of a proper copolymer end effect. In addition, difficulties arise in determining univocal triads of reliable values for the structural parameters from the four-parameter equation $(7)^{31}$.

Finally, it should be noted that discussion is still in progress about a possible piecewise or segmented form of the $T_{\rm g}$ -x relation from experimental data represented by equation (6)^{25,29} or otherwise^{18,20,32-37}.

Star polymers

An interesting case of non-linear polymers is that of star polystyrenes, studied by Roovers and Toporowski²¹ with the aim of clarifying the relation between T_g and

'end-group concentration'. The structure of the end units of their star samples (styryl) was very close to that of the chain units. Thus, strictly speaking on the lines of the present work, this is a particular case of copolymers (the central unit of the body greatly different from the chain units) practically devoid of a chemical dissimilarity end effect (end units very similar to the chain units). These authors²¹, by analysing their results in terms of equation (1), found that the (positive) K values for their four- and six-branched star polymers are respectively about two and three times those for linear polystyrenes. The influence of the end groups was, therefore, investigated on the basis of their number per molecule, and not from the point of view of a (practically absent) chemical dissimilarity.

T_{g-x} OF POLYMERS AND COPOLYMERS WITH FOREIGN END UNITS

Previous results

A definite end effect of a chemical dissimilarity of end units was studied and reported by Ueberreiter and Rohde-Liebenau³⁸ in 1961. Using a particular radical initiator, they synthesized polystyrenes rich in decidedly foreign end groups (trichloro-triphenyl-methyl groups) and found some slightly positive $T_{\rm g}$ deviations from the asymptotic value with decreasing x, instead of marked negative deviations, as expected for 'normal' polystyrenes. As far as we know, this is the only example in the literature of observed positive $T_{\rm g}$ deviations, surprisingly ignored in subsequent literature (apart from the recent different case, examined above, of cyclic polymers¹⁻³).

Some evidence of a chemical dissimilarity end effect on $T_{\rm g}$ was recently pointed out by Tadlaoui et al.³⁷. Using mercaptan chain transfer reagents, they radically synthesized methyl methacrylate telomers with different end groups (C_6H_5S - or $C_8F_{17}C_2H_4S$ -) and found marked negative $T_{\rm g}$ deviations, however claimed as different from those 'of a standard' poly(methyl methacrylate).

Our results

Our T_g measurements were made on five series of oligomers of different molecular weights, having the same perfluorinated body (PFB) and two equal foreign end groups E of five different types.

The system has the general constitution E-CF₂O[(CF₂ CF₂O)_p (CF₂O)_q]CF₂-E, abbreviated to E(PFB)E, with degree of polymerization $x = x_{\rm M} + 2$ (i.e. $x = x_{\rm M}$ monomeric units + 2 end units), where $x_{\rm M} = p + q + 1$, substantially consisting of a non-crystallizable, random copolymeric body (a perfluoro poly(oxymethylene-oxyethylene) chain, having a ratio p/q between 0.91 and 1.11) with two equal end groups or units of one of the following types: -CH₂OCH₃; -CH₂OSi(CH₃)₃; -CH₂OCOCF₃; -CH₂OH; -CH₂OK.

The diolic $HOCH_2(PFB)CH_2OH$ series was first investigated with several samples of different x_M . Four were samples of Fomblin-ZDOL^R (Ausimont SpA, Montedison Specialty Chemicals, Milan), having $M_n = 700-3700$, and M_w/M_n in the range 1.19–1.50. From these base samples, others were obtained by fractional separation using distilled Delifrene-LS^R (Ausimont) as solvent, and methanol or CH_2Cl_2 as non-solvent. The data relating to this diolic series are collected in Table 1. In Figure 1a the T_R values are plotted against x_M .

Table 1 Characterization of the fractions of the diolic series HOCH₂(PFB)CH₂OH

Fraction	p/q	$M_{\rm w}/M_{\rm n}$	M_{n}	x_{M}	f_{M}	T _g (°C)	$T_{\mathbf{g}}$ (K)
F12	0.96	1.07	350	2.90	0.592	-81.0	192.1
F11 ^a	0.96	1.29	700	6.77	0.772	-97.5	175.6
F10 ^a	0.91	1.19	1150	11.82	0.855	-107.0	166.1
F9	0.93	1.37	1950	20.67	0.912	-113.2	159.9
F8ª	1.02	1.50	2100	22.06	0.917	-113.9	159.2
F7	1.04	1.21	3250	34.58	0.945	-117.0	156.1
F6	1.10	1.10	3500	37.03	0.949	-117.2	155.9
$F5^a$	1.03	1.40	3700	39.55	0.952	-117.9	155.2
F4	1.11	1.05	3900	41.32	0.954	-117.3	155.8
F3	1.09	1.16	4300	45.77	0.958	-117.9	155.2
F2	1.01	1.16	8000	86.84	0.977	-120.8	152.3
F1	0.99	1.23	10600	115.69	0.983	-121.1	152.0

^a Base samples of Fomblin-ZDOL

Portions of the four base samples were then derivatized by reaction with dimethylsulfate, hexamethyldisilazane, trifluoroacetic anhydride and potassium t-butoxide, respectively, (all Aldrich reagents), in order to investigate diversified end-capped series. The data relating to these series are reported in Table 2, and the $T_{\rm g}$ values graphically represented in Figure 1b as a function of $x_{\rm M}$.

In Tables 1 and 2, all the $M_{\rm n}$ data were calculated from $^{19}{\rm F}$ n.m.r. spectra (Varian 200 MHz), in good agreement with results obtained from v.p.o. measurements (Hitachi–Perkin-Elmer-115). The $M_{\rm w}/M_{\rm n}$ ratio was determined by g.p.c. (Waters-5900). The $T_{\rm g}$ data were recorded by d.s.c. (Mettler TA 3000) in a cooling run from 35 to $-170^{\circ}{\rm C}$, at $10^{\circ}{\rm C}$ min $^{-1}$.

From our results it immediately appears that the $T_{\rm g}$ -x relation for a given polymeric system (with a common molecular body) can be heavily modified by changing the chemical nature of the end groups or units. Qualitatively, the experimental data are by themselves expressive from a phenomenological point of view; both positive and negative $T_{\rm g}$ deviations can take place. Quantitatively, the data do not encompass x values below that of a body trimer, and for four series the data are relatively few, so that it is convenient at present to limit our discussion to the possible validity of the simplest, two-parameter equations (1) and (2).

For our purposes equation (1) can be rewritten as follows:

$$T_{\rm g} = T_{\rm g}(\infty) + \frac{2D}{x_{\rm M} + 2} \qquad (0 \leqslant x_{\rm M} \leqslant \infty)$$
 (8)

or alternatively:

$$\Delta T_{\rm g} = T_{\rm g} - T_{\rm g}(\infty) = \frac{2D}{x_{\rm M} + 2} \tag{8'}$$

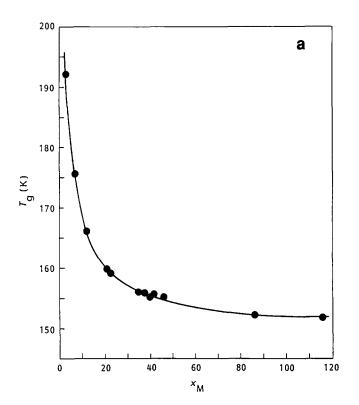
where D is a parameter expressing, for any given pair of end groups, the sign and extent of the T_g deviations from the (parametric) $T_g(\infty)$ asymptotic value of the chosen polymeric body.

Figure 2 shows the T_g data relating to the diolic $HOCH_2(PFB)CH_2OH$ series when linearly plotted according to equation (8).

A corresponding result can be obtained starting with equation (2), evidently because the experimental accuracy in the investigated x interval lies in the purely mathematical differences between the $T_{\rm g}$ values predicted

by equations (1) and (2) (as already apparent from previous literature on other systems). Thus, for the diolic series (with positive T_g deviations), in the x range examined ($x \ge 5$), equations (1) and (2) can be considered as valid (as previously observed for several other systems with negative T_g deviations, at 'sufficiently high' x values).

Figure 3 shows the ΔT_g experimental results of Table 2 linearly plotted according to equation (8'). By



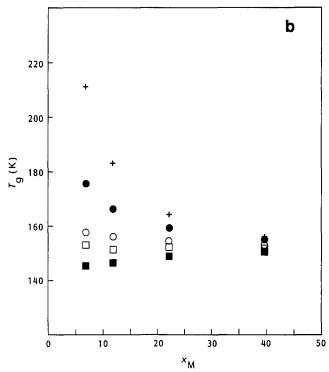


Figure 1 Relation between T_g and body degree of polymerization x_M of: (a) the diolic series of fractions $HOCH_2(PFB)CH_2OH$ (data of Table 1); (b) the five end oligomeric series examined (data of Table 2):

, met; \Box , sil; \bigcirc , acf; \bigcirc , dol; +, ok; end group abbreviations as in Table 2

Table 2 Characterization of the four fractions of the five different end oligomeric series examined

Fraction ^a	p/q	$M_{\rm w}/M_{\rm n}$	x_{M}	T _g (°C)	T _g (K)	$\Delta T_{ m g}$
met 1 sil 1 acf 1 dol 1 ok 1	0.96	1.29	6.77	-127.8 -120.0 -115.4 -97.5 -62.2	145.3 153.1 157.7 175.6 211.0	-5.9 1.9 6.5 24.4 59.75
met 2 sil 2 acf 2 dol 2 ok 2	0.91	1.19	11.82	-126.6 -121.6 -117.0 -107.0 -90.0	146.5 151.5 156.1 166.1 183.1	-4.7 0.3 4.9 14.9 31.9
met 3 sil 3 acf 3 dol 3 ok 3	1.02	1.50	22.06	-124.2 -120.7 -118.5 -113.9 -109.0	148.9 152.4 154.6 159.2 164.1	-2.3 1.2 3.4 8.0 12.9
met 4 sil 4 acf 4 dol 4 ok 4	1.03	1.40	39.55	-122.5 -121.3 -120.1 -117.9 -117.4	150.6 151.8 153.0 155.2 155.7	-0.6 0.6 1.8 4.0 4.5

^a End groups: $met = CH_2OCH_3$; $dol = CH_2OH$; $sil = CH_2OSi(CH_3)_3$; $ok = CH_2OK$; $acf = CH_2OCOCF_3$

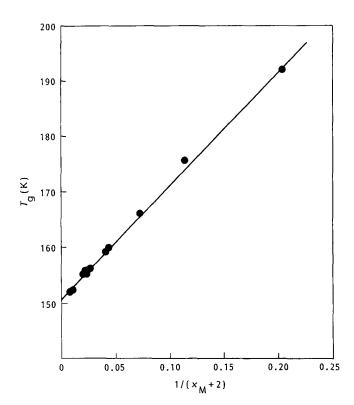


Figure 2 Plot of T_8 against $1/(x_M+2)$, according to equation (8), of the diolic series $HOCH_2(PFB)CH_2OH$ (data from Table 1)

assuming, as a first approximation, strictly linear behaviour, from a least-squares fitting one obtains $T_{\rm g}(\infty)=151~{\rm K}$ and the following most probable values for the deviation parameter D for each specified end group: $-{\rm CH_2OCH_3}, -26; -{\rm CH_2OSi(CH_3)_3}, +9; -{\rm CH_2OCOCF_3}, +32; -{\rm CH_2OH}, +102.$

With the fifth end-group type, giving the largest positive deviations, a linear interpolation is clearly unacceptable, so that for -CH₂OK, D is largely positive,

increasing with decreasing x. This behaviour might indicate that for all the series a curved $T_{\rm g}-1/x$ trend could be more realistic, in fact experimentally detectable only when the $T_{\rm g}$ deviations are comparatively large.

All these results suggest that in our case the end effect is prevalently determined by (probably polar) surcohesion phenomena, and less by the geometric features of the end groups.

On this basis we can interpret the $T_{\rm g}$ data of Marchionni et al.²⁹ for a series of samples (Fomblin-Z^R) having a perfluorinated body similar to that of our system, and end groups $-{\rm OCF}_3$. Although in a range of somewhat higher x, they show a trend of marked negative deviations, comparatively greater than the negative ones observed in our system (with $E=-{\rm CH}_2{\rm OCH}_3$). The $-{\rm OCF}_3$ end groups are very similar in chemical nature to the body, so that this case may be seen as very close to a reference, from an infinite chain 'scissor-made' molecular model, with the minimal foreign-end-unit effect, and an easier theoretical interpretation. At present, this comparison may generally be assumed as a criterion for a quantitative evaluation of the chemical dissimilarity end effect.

An interesting physical meaning of the parameter D can be suggested by the copolymeric view of the end effect. Every oligomeric or polymeric compound may be seen as belonging to an 'end copolymeric system', in our case: $EM_{x_M}E$ (generally $E'M_{x_M}E''$), whose extreme pure components are M_{∞} on one side, and E_2 on the other, having T_g values: $T_g(\infty)$ and $T_g(E)$ respectively. Its composition can be expressed by the molar fraction of the different M and E units:

$$f_{\mathsf{M}} = \frac{x_{\mathsf{M}}}{x_{\mathsf{M}} + 2} \qquad f_{\mathsf{E}} = \frac{2}{x_{\mathsf{M}} + 2}$$

By assuming (to a first approximation) equation (8) as

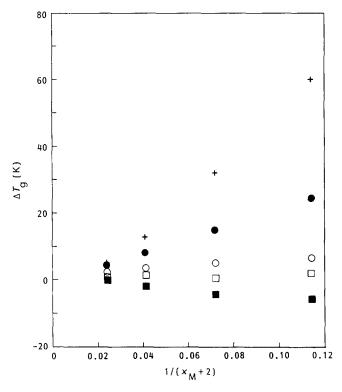


Figure 3 T_g deviations (ΔT_g) of the five end copolymeric series examined as a function of $1/(x_M+2)$, according to equation (8'): \blacksquare , met; \square , sil; \bigcirc , acf; \bigcirc , dol; +, ok; end group abbreviations as in *Table 2*

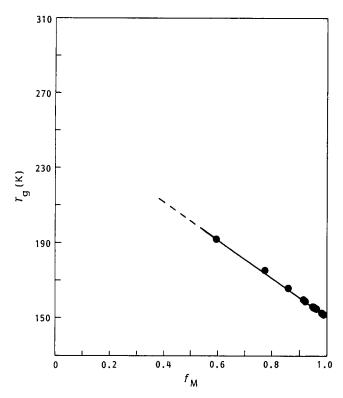


Figure 4 End copolymer composition diagram representing T_g (according to equation (10)) of the diolic series HOCH₂(PFB)CH₂OH

valid over the whole range of x_M , when $x_M = 0$, $T_g = T_g(E)$; it follows that:

$$D = T_{o}(E) - T_{o}(\infty) \tag{9}$$

i.e. D represents the difference between the $T_{\rm g}$ of the component E_2 and that of the component M_{∞} (D being positive when $T_{\rm g}(E) > T_{\rm g}(\infty)$). Equation (8) can thus be rewritten as:

$$T_{\rm g} = T_{\rm g}(\infty) + \frac{2[T_{\rm g}(E) - T_{\rm g}(\infty)]}{x_{\rm M} + 2}$$
 (8")

Hence, by expressing $x_{\rm M}$ in terms of composition, the following 'end copolymer composition equation' can be derived:

$$T_{\mathbf{g}} = T_{\mathbf{g}}(\mathbf{E}) + (T_{\mathbf{g}}(\infty) - T_{\mathbf{g}}(\mathbf{E}))f_{\mathbf{M}}$$
 (10)

or, in a distributive form:

$$T_{\mathbf{g}} = T_{\mathbf{g}}(\infty) f_{\mathbf{M}} + T_{\mathbf{g}}(\mathbf{E}) f_{\mathbf{E}} \tag{10'}$$

In Figure 4 the $T_{\rm g}$ data of the diolic series are plotted according to equation (10) as a function of $f_{\rm M}$; they are indeed well represented by a straight line.

With the present knowledge it is of course hardly possible to predict the limits of reliability of such a relation, because of lack of experimental data at the lowest x, i.e. $f_{\rm M}$ values, largely expanded for a few oligomers on the left of Figure 4.

An attempt to evaluate equation (10) may be made by calculating $T_g(E)$ from D using equations (8) and (9), and comparing this value to that of the T_g of the pure E_2 component. For the diolic series, for example, equation (9) gives $T_g(E) = 253 \text{ K}$, but the T_g of ethylene glycol (estimated with the Tammann rule: $T_g = 2/3T_m$) should be about 170 K, i.e. much smaller than that calculated. However, for the series with end groups $-CH_2OCH_3$, the

calculated value is 125 K, relatively close to 143 K, which can be estimated for CH₃OCH₂CH₂OCH₃. No better agreement can be obtained starting with equation (2) instead of equation (1).

CONCLUSIONS

The effect definitely demonstrated of the molecular end groups or units having chemical structures different from that of the body units on the $T_{\rm g}$ of a polymeric system, reliably measurable in the x range of oligomeric values, appears to be substantial and must be taken into full consideration. Various theoretical treatments of the $T_{\rm g}-x$ relation, briefly reviewed in this paper, clearly should be either revised or better specified in order to explicitly take into account this 'copolymer end effect'.

From an intuitive, physical point of view, the glass transition temperature has to be related to a whole cohesion state of the system, and not uniquely to a cohesive energy^{39,40} or to (intrinsic or consequent) degrees of freedom²⁰. Thus, as a quite general remark, it might be said that, in principle, a lowering of the molecular weight of a polymeric system should result by itself in important structural changes generally implying a kind of discohesion of the matter constituting the system itself. Major structural changes can, however, be brought about by the chemical nature and size of the progressively ensuing end groups or units by decreasing x. Good compatibility, for example, between end groups and body can improve cohesion, whereas poor compatibility can enhance discohesion, but, at the limit, can give rise to end molecular associations. These may result either in a surcohesion, or in further discohesion, depending on the relative intensities of body/body and end/end affinities. Furthermore, incompatibility leads to substantial morphological changes, such as sub-phase or phase separations of different order, degree or size scale in the originally homogeneous systems or sub-systems, with an outstanding variety of possible ensuing structures, and consequent effects on their properties, increasing as the molecular weight decreases.

Clearly, such a variety of phenomenological possibilities can make the form of the $T_{\rm g}-x$ relation particularly complex, and complicate its theoretical interpretation in the delicate range of the lowest x values, in which the copolymer end effect becomes dominant, in addition to possible abrupt changes of structural regime which are still under discussion.

ACKNOWLEDGEMENTS

Thanks are due to Ausimont SpA, Milan, and in particular to Drs M. Malavasi and D. Sianesi, for their consideration and support regarding this present work. A financial contribution was also given by the University MURST (60%) Fund, Rome.

REFERENCES

- Clarson, S. J., Dodgson, K. and Semlyen, J. A. *Polymer* 1985, 26, 930
- 2 Hogen-Esch, T. E. and Toreki, W. Polymer Prepr. 1988, 30 1), 129
- 3 Clarson, S. J., Semlyen, J. A. and Dodgson, K. Polymer 1991, 32, 2823
- 4 Di Marzio, E. A. and Guttman, C. M. Macromolecules 1987, 20, 1403

- Gibbs, J. H. and Di Marzio, E. A. J. Chem. Phys. 1958, 28, 373
- 6 7 Ehrenfest, P. Proc. Acad. Amsterdam 1933, 36, 153
- Beevers, R. B. and White, E. F. T. Trans. Faraday Soc. 1960, 56,
- 8 Cowie, J. M. G. and Toporowski, P. M. Eur. Polym. J. 1968, 4, 621
- 9 Pezzin, G., Zilio-Grandi, F. and Sanmartin, P. Eur. Polym. J. 1970, **6**, 1053
- 10 Di Marzio, E. A. Ann. N. Y. Acad. Sci. 1981, 371, 1
- Di Marzio, E. A. in 'Relaxation in Complex Systems', (Eds K. L. Ngai and G. B. Wright) NTIS, USDOC, Springfield, 11 VA, 1986, pp. 43-52
- Cowie, J. M. G. and McEwen, I. J. Polymer 1973, 14, 423 12
- 13
- Fox, T. G. and Flory, P. J. J. Appl. Phys. 1950, 21, 581 Ueberreiter, K. and Kanig, G. J. Colloid Sci. 1952, 7, 569
- Ueberreiter, K. and Kanig, G. Z. Naturforsch., Teil A 1951, 15 6, 551
- Schulz, G. V., von Guenner, K. and Gerrens, H. Z. Phys. Chem. 16 1955, 4, 192
- 17 Fox, T. G. and Loshaek, S. J. Polym. Sci. 1955, 15, 371
- Gillham, J. K. and Boyer, R. F. J. Macromol. Sci., Phys. 1977, 18
- 19 Boyer, R. F. Macromolecules 1974, 7, 142
- Vilgis, T. A. Polym. Commun. 1988, 29, 327 20
- 21 Roovers, J. E. L. and Toporowski, P. M. J. Appl. Polym. Sci. 1974, 18, 1685
- 22 Kelley, F. N. and Bueche, F. J. Polym. Sci. 1961, 50, 549

- Somcynsky, T. and Patterson, D. J. Polym. Sci. 1962, 62, 151
- Kanig, G. Kolloid Z. Z. Polym. 1963, 190, 1 24
- 25 Lee, M. C. H. and Williams, M. C. J. Macromol. Sci. Phys. 1987, 26, 145
- 26 Lee, M. C. H. and Williams, M. C. J. Polym. Sci., Polym. Phys. Edn 1985, 23, 2243
- 27 Fox, T. G. and Flory, P. J. J. Polym. Sci. 1954, 14, 315
- Rudin, A. and Burgin, D. Polymer 1975, 16, 291 28
- 29 Marchionni, G., Ajroldi, G., Righetti, M. C. and Pezzin, G. Polym. Commun. 1991, 32, 71
- 30 Di Benedetto, A. T. J. Polym. Sci. 1987, 25, 1949
- 31 Di Benedetto, A. T. and Di Landro, L. J. Polym. Sci. 1989, 27, 1405
- 32 Cowie, J. M. G. Eur. Polym. J. 1975, 11, 297
- 33 Turner, D. T. Polymer 1978, 19, 789
- Chandry, P., Letoffe, J. M., Camberlin, Y. and Pascault, J. P. Polym. Bull. 1983, 9, 208
- 35 Boutevin, B., Snoussi, M. H. and Taha, M. Eur. Polym. J. 1985, 21, 445
- 36 Boutevin, B., Pietrasanta, Y., Sarraf, L. and Snoussi, M. H. Eur. Polym. J. 1988, 24, 539
- 37 Tadlaoui, K., Pietrasanta, Y., Michel, A. and Verney, V. Polymer 1991, 32, 2234
- 38 Ueberreiter, K. and Rohde-Liebenau, U. Makromol. Chem. 1961, **49**, 164
- 39 Hayes, R. A. J. Appl. Polym. Sci. 1961, 5, 318
- 40 Lee, W. A. and Sewell, J. H. J. Appl. Polym. Sci. 1968, 12, 1397